

computing a least upper bound for the bandwidth used in an MPLS-based VPN; and

combining the upper bound and the lower bound to produce an estimate for the cost of the bandwidth.

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4. The computer program method of claim 3, wherein the step of computing a least upper bound includes a cut constraint.

5. A method for calculating an approximate cost of multi-protocol label switching (MPLS) based virtual private network (VPN) services, comprising:

computing a greatest lower bound for the bandwidth used in an MPLS-based VPN, comprising the steps of:

- (a) Creating an auxiliary graph of Start and Finish nodes and one node for each node in the VPN that is saturated with inbound flow;
- (b) Creating a directed edge between the nodes representing a least cost of adding flow from a node which has flow left to place to a node which has capacity to receive the flow;
- (c) Calculating a shortest path algorithm to find the path from Start and Finish nodes giving an optimal way of serving the previously unserved unit of flow.
- (d) Outputting L as a greatest lower bound for the bandwidth used;

computing a least upper bound for the bandwidth used in an MPLS-based VPN, comprising the steps of:

- (e) Creating an auxiliary graph consisting of the nodes Start, Finish, and one node for each node in the VPN that is saturated with inbound flow;

- (f) Creating a directed edge between the nodes representing a greatest cost of adding flow from a node which has flow left to place to a node which has capacity to receive the flow;
- (g) Calculating a longest path algorithm to find the path from Start to Finish, giving a
5 worst way of serving the previously unserved unit of flow;
- (h) Outputting U as a least upper bound for the bandwidth used;

combining the upper bound and the lower bound to produce an estimate for the cost of the bandwidth, comprising the step of:

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- (i) setting a $\text{Total_cost} \approx \alpha \times U + (1 - \alpha) \times L$
where α is a measure of risk of losing money by carrying a given customer's VPN.

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